Fifth Semester B.E. Degree Examination, Dec.2013/Jan.2014 **Digital Signal Processing**

Time: 3 hrs. Max. Marks: 100

> Note: Answer FIVE full questions, selecting at least TWO questions from each part.

- Given the following x(n) : $x(n) = \frac{\mathbf{PART} \mathbf{A}}{\delta(n) + \delta(n-1) + \delta(n-2)}$
 - (i) Find the Fourier transform $X(e^{jw})$ and plot the $[X(e^{jw})]$
 - (ii) Get the magnitude of the 4-point DFT of the first four samples of x(n)
 - (iii) Get the magnitude of the 8-point DFT of the first eight samples of x(n)(10 Marks)
 - Find the 4-point DFT of the sequence, $x(n) = 6 + \sin \frac{2\pi n}{4}$, $0 \le n \le 3$. (06 Marks)
 - c. Consider the sequence $\mathbf{x}_1(n) = (0,1,2,3,4)$ and $\mathbf{x}_2(n) = (0,1,0,0,0)$. Determine the sequence y(n) so that $Y(K) = X_1(K) X_2(K)$. $X_1(K)$ and $X_2(K)$ are 5-point DFTs of $x_1(n)$ and $x_2(n)$ respectively. (04 Marks)
- a. A sequence $x(n) = \begin{cases} 1 & 0 \le n \le 3 \\ 0 & 4 \le n \le 7 \end{cases}$ has an 8-point DFT X(K). Compute the DFT of $x_2(n)$ and $x_3(n)$ in terms of X(K), for

$$\mathbf{x}_{2}(\mathbf{n}) = \begin{cases} 1 & \mathbf{n} = 0 \\ 0 & 1 \le \mathbf{n} \le 4 \text{, } \mathbf{x}_{3}(\mathbf{n}) = \begin{cases} 0 & 0 \le \mathbf{n} \le 1 \\ 1 & 2 \le \mathbf{n} \le 5 \\ 0 & 6 \le \mathbf{n} \le 7 \end{cases}$$
 (06 Marks)

- b. Consider a sequence x(n) = (8, 3, 4, 1, -5, -4, -2, 0, 2, -1, 7, 4). Evaluate the following without explicitly computing X(K).
 - (i) DFT[DFT[DFT[x(n)]]]
 - (ii) $\sum_{K=0}^{11} X(K)$

(iii)
$$\sum_{K=0}^{11} e^{\frac{-j\pi K}{6}} X(K)$$
 (10 Marks)

c. x(t) is an analog signal having a bandwidth of 4 kHz. It is desired to compute the spectrum of this signal using $N = 2^{M}$ point DFT with a resolution better than or equal to 50 Hz. Determine the minimum sampling rate and the resulting resolution (M is an integer).

(04 Marks) 🧷 💃

- 3 1) to an input x(n) = (2, 1, -1, -2, -3, 5, 6, -1, 2, 0, 2, 1). Use only 8-point circular convolution. Can the system exhibit linear phase? (12 Marks)
 - Show that the product of two complex numbers (a+jb) and (c+jd) can be performed with three real multiplications and five additions. (04 Marks)
 - Bring out a comparison between linear convolution and circular convolution. (04 Marks)

- 4 a. Using DIFFFT algorithm, compute DFT of the sequence, x(n) = (1, 2, -1, 2, 4, 2, -1, 2)
 - If $x_1(n)=x(n-4)_8$, compute $x_1(K)$ without invoking FFT algorithm. (14 Marks)
 - b. Compute the DFT of the sequence x(n) = (1, 2, 1, 2) using the Goertzel algorithm. (06 Marks)

PART - B

- 5 a. Show that the bilinear transformation maps.
 - (i) The $j\Omega$ axis in s-plane onto the unit circle, |z| = 1.
 - (ii) The left half s-plane, Re(s)<0 inside the unit circle, |z|<1 (08 Marks)
 - b. Design a digital low-pass filter using the bilinear transformation method to satisfy the following characteristics: (i) Monotonic stopband and passband (ii) -3.01 dB cut off frequency of 0.5π rad; (iii) Magnitude down at least 15 dB at 0.75π rad. (08 Marks)
 - c. Bring out a comparison between Butterworth filter and Chebyshev filter. (04 Marks)
- 6 a. Transform $H(s) = \frac{s+a}{(s+a)^2 + b^2}$ into a digital filter using impulse invariance technique.

(08 Marks)

- b. Let $H(s) = \frac{1}{s^2 + \sqrt{2}s + 1}$, for a 2^{nd} order low pass Butterworth filter prototype. Determine the system function for the digital bandpass filter using bilinear transformation. The cutoff frequencies for the digital filter should be at $\omega_L = \frac{5\pi}{12}$ and $\omega_u = \frac{7\pi}{12}$. Take T = 2. (08 Marks)
- c. What does linear phase do to the response of an input signal within the passband of the filter? Why choose an IIR filter instead of an FIR filter? (04 Marks)
- Find the unit sample response of a symmetric FIR filter having a length of 9 samples. The desired frequency response is given by, $H_{\alpha}(\omega) = e^{-\gamma \omega \alpha} \quad |\omega| \le \omega_{C}, \text{ where } \omega_{C} = \frac{\pi}{2} \text{ and } \omega \ge \omega_{C}$

 $\omega_{\text{Hanning}}\left(n\right) = \frac{1}{2} \left[1 - \cos\left(\frac{2\pi n}{N-1}\right)\right], \quad 0 \leq n \leq (N-1) \text{ . Also find H(z), linear constant coefficient difference equation and the frequency response H(e^{j\omega}). Draw the structure of the filter.}$

(20 Marks)

8 a. Obtain the series and parallel form realization for a digital filter described by the system function.

$$H(z) = \frac{8z^3 - 4z^2 + 11z - 2}{\left(z - \frac{1}{4}\right)\left(z^2 - z + \frac{1}{2}\right)}.$$
 (14 Marks)

b. Determine the parameters K_m of the lattice filter corresponding to the FIR filter described by,

$$H(z) = 1 + 2.82z^{-1} + 3.408z^{-2} + 1.74z^{-3}$$
 (06 Marks)

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